

# $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ measurement from BNL's E949



For the E949 collaboration:  
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New Opportunities in Kaon Physics  
Birmingham, UK, Nov 27 2008

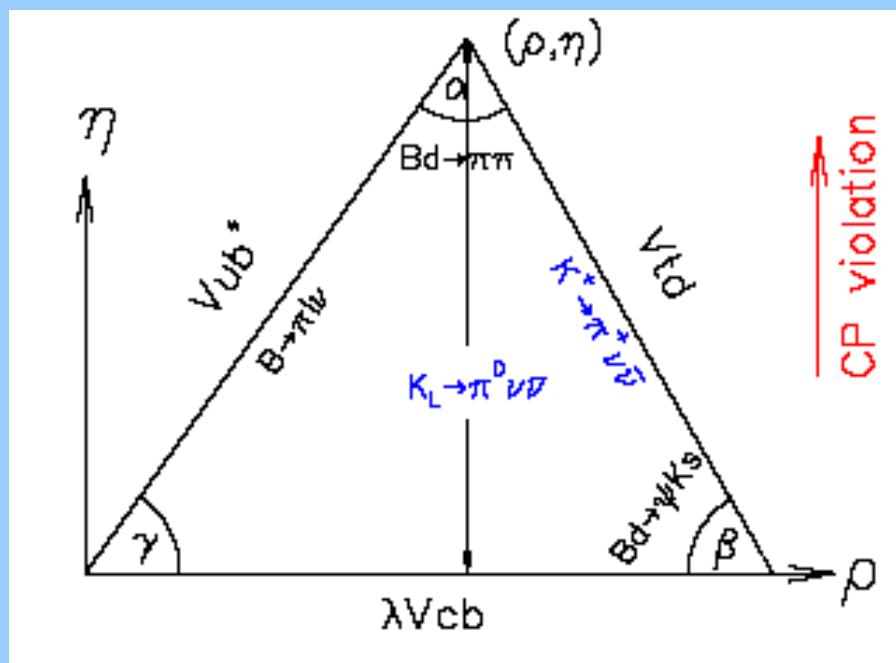
# Outline

- Motivation, current status of CKM measurements, the Standard Model  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$  BR
- The measurement with the E949 detector
  - Background overview
  - Detector and measurement method
  - Peculiarities of the PNN2 region
- The analysis
  - Strategy and tools
  - The 2 major backgrounds
  - Cross-check methods
  - Expected background and likelihood ratio method
- The result
  - This analysis
  - Past (E787, E949 PNN1) results
  - Combined E949-E787 result

# Motivation

$K^+ \rightarrow \pi^+ \nu \bar{\nu}$  is the rarest process ever detected in Particle Physics. It can give a direct and independent measurement of  $|V_{td}|$ , the smallest and most elusive element of the CKM matrix

The Kaon Unitarity triangle:  $V_{ud} V_{ub}^* + V_{cd} V_{cb}^* + V_{td} V_{tb}^* = 0$



Processes w/ small theoretical uncertainties:

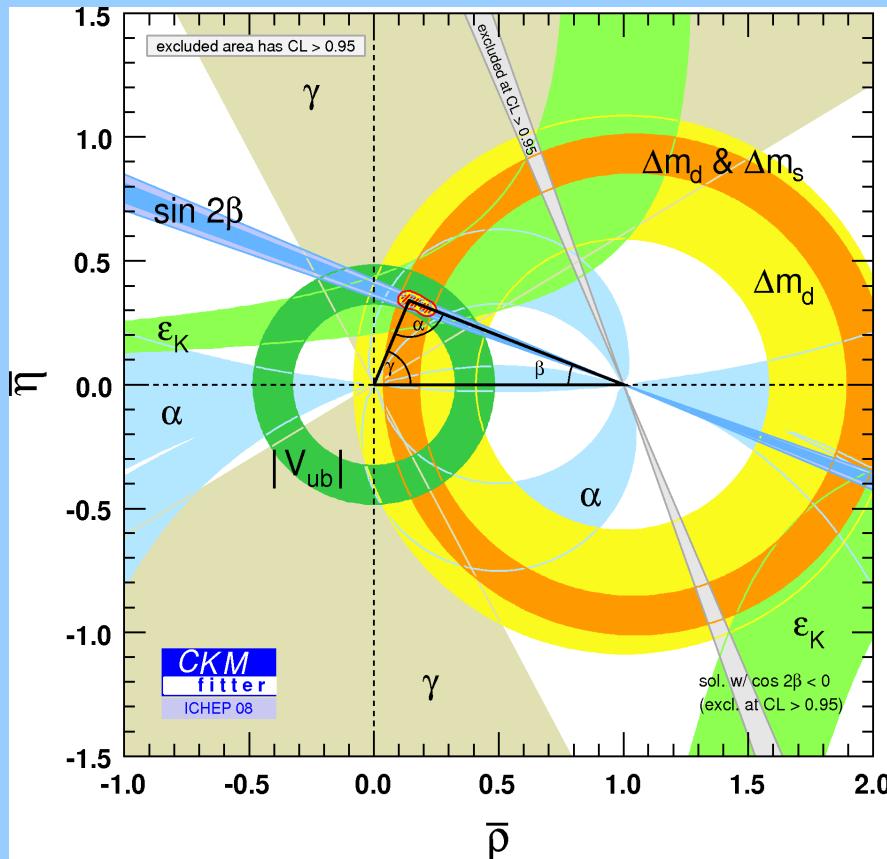
Process	Experiments
$\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu})$	E787/E949, FNAL-E921
$\mathcal{B}(K_L^0 \rightarrow \pi^0 \nu \bar{\nu})$	KOPIO, E391a
$\mathcal{A}(B \rightarrow J/\psi K_S^0)$	BaBar, Belle

CP violating decay rate asymmetry

$\Delta M_{B_s}/\Delta M_{B_d}$	CDF, D0, LHCb, BTeV
---------------------------------	---------------------

ratio of mixing frequencies of  $B_s$  and  $B_d$  mesons

# Measurements of unitarity triangle



$|V_{ub}|, |V_{cb}|$  : tree-level semileptonic B decays

$|V_{td}|$  :  $\Delta M_{Bs} / \Delta M_{Bd}$  &  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$

$\sin 2\beta$  (&  $2\alpha$ ) : CP asymmetry in hadronic B decays  $A(B_d \rightarrow J/\psi K^0)$  &  $\text{BR}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) / \text{BR}(K^0 \rightarrow \pi^0 \nu \bar{\nu})$

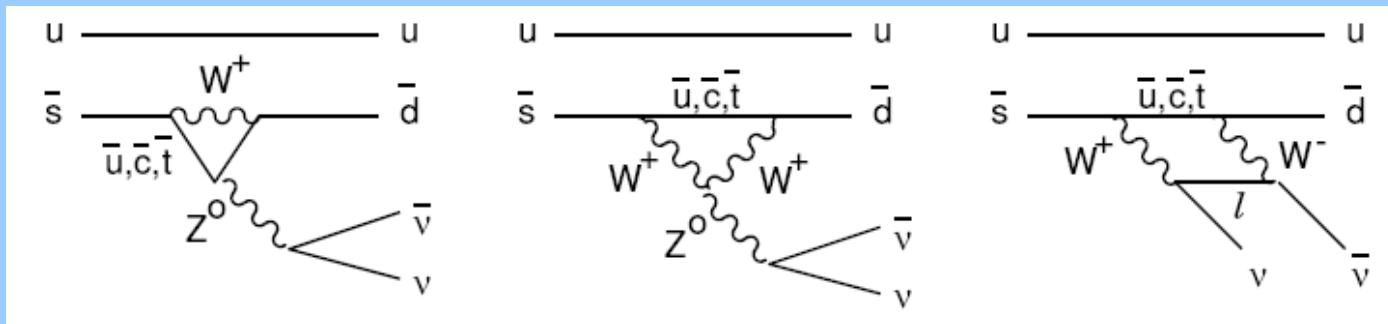
$\epsilon_K$  : CP violation in the K sector

CKMfitter Group (J. Charles et al.), Eur. Phys. J. C41, 1-131 (2005) [hep-ph/0406184], updated results and plots available at: <http://ckmfitter.in2p3.fr>

A better determination of  $V_{td}$  from  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$  will provide a sensitive test of the SM by comparing the results from the K and B sector and probe new physics

# The SM $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ BR

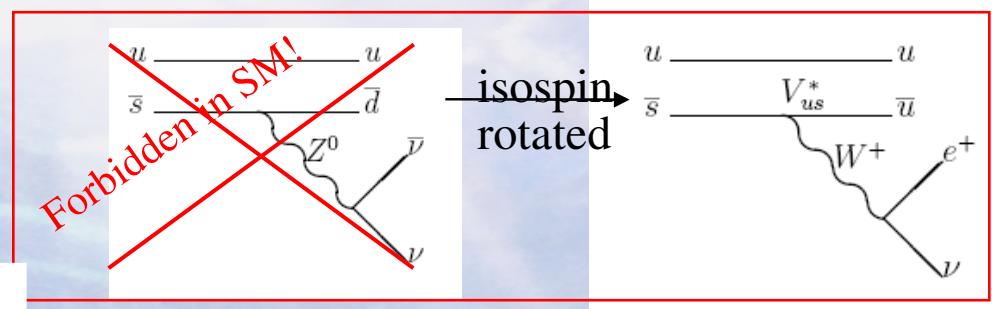
- All processes at 2<sup>nd</sup> order, with main contribution of t in the loop
- Very clean calculation (precision < 5%, uncertainties mainly from c sector)



$$BR(K^+ \rightarrow \pi^+ \nu \bar{\nu}) \propto \sum_{l=e,\mu,\tau} \left| \left[ V_{cs}^* V_{cd} X(\chi_c) + V_{ts}^* V_{td} X(\chi_t) \right] \times \underbrace{(H A D R)}_{\text{isospin rotated}} \times (\bar{\nu}_l \nu_l) \right|^2 \Rightarrow$$

$\dots BR \propto (\sigma \eta)^2 + (\rho_\phi - \bar{\rho})^2 \rightarrow \text{ellipse in } \rho\text{-}\eta \text{ plane}$

$$\sigma = \left( \frac{1}{1 - \lambda^2 / 2} \right)^2$$



$$BR_{th}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (0.84 \pm 0.7) \times 10^{-10}$$

# The E949 collaboration

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TRIUMF

Students and post-docs in red.

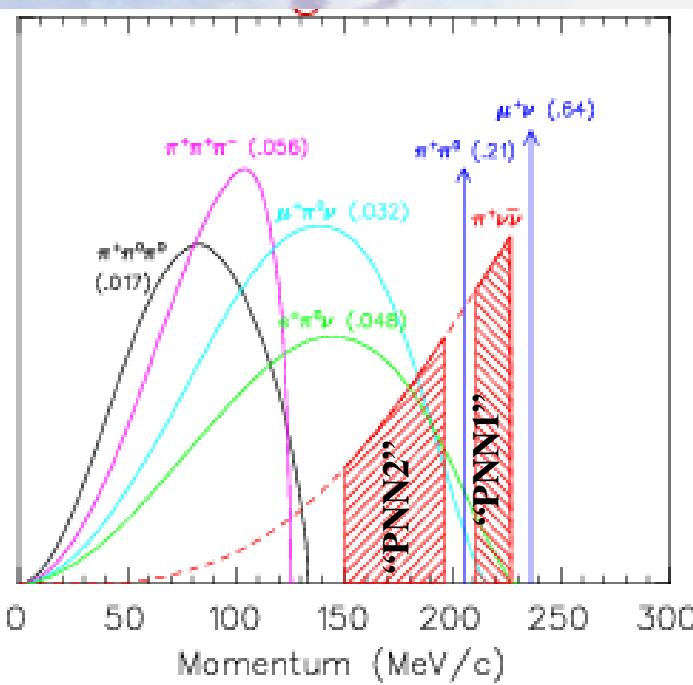
~70 physicists, plus a lot of hard work from earlier E787 collaborators.



# The measurement, backgrounds

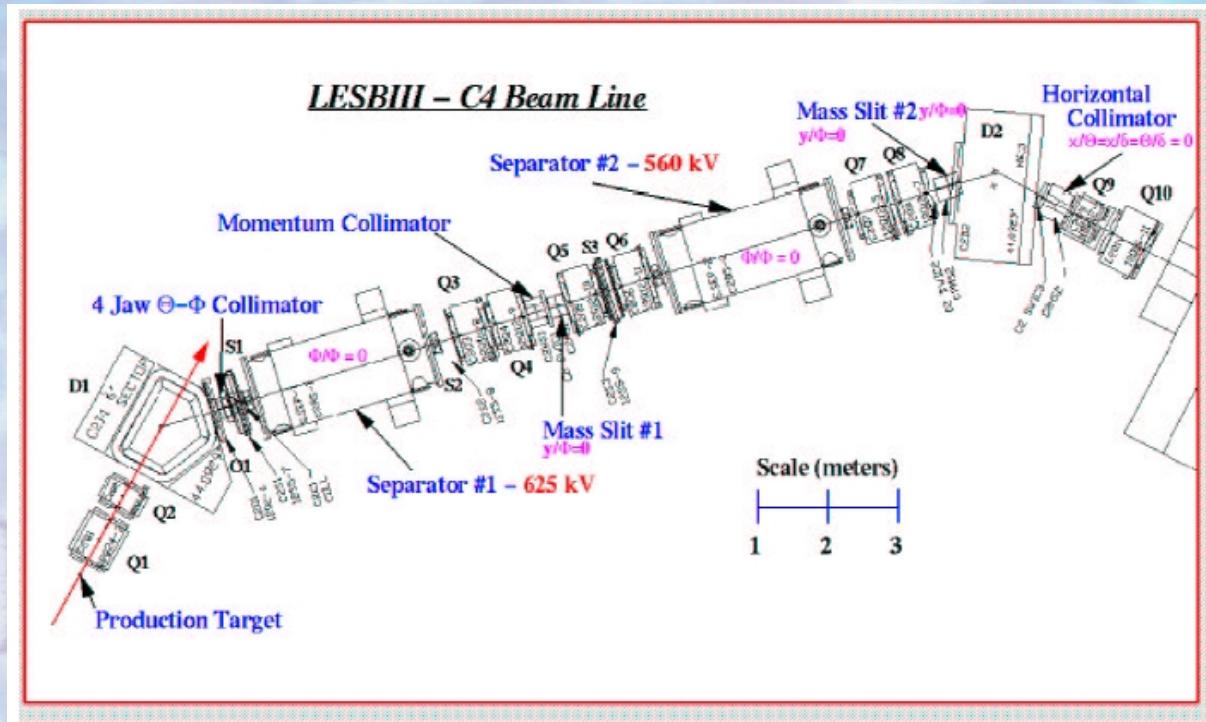
- 3-body decay w/ 2 missing particles:  $0 \leq p_{\pi^+} \leq 227 \text{ MeV}/c \Rightarrow$   
Signal:  $\Pi^+ + \text{nothing}$ , backgrounds need to be vetoed  $\sim 10^{-11}$  !
- Need
  - particle identification (PID)
  - all other charged particles vetoed  $< 10^{-3}$
  - redundant precise kinematic measurements

*Latest result on PNN2  
will be presented*



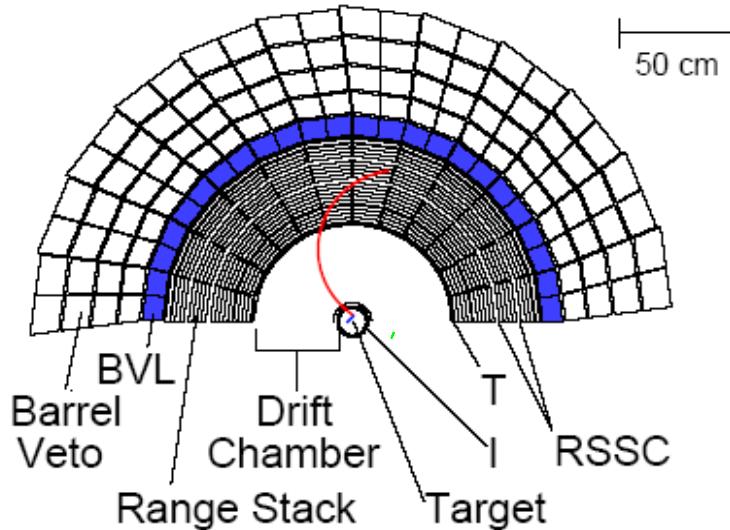
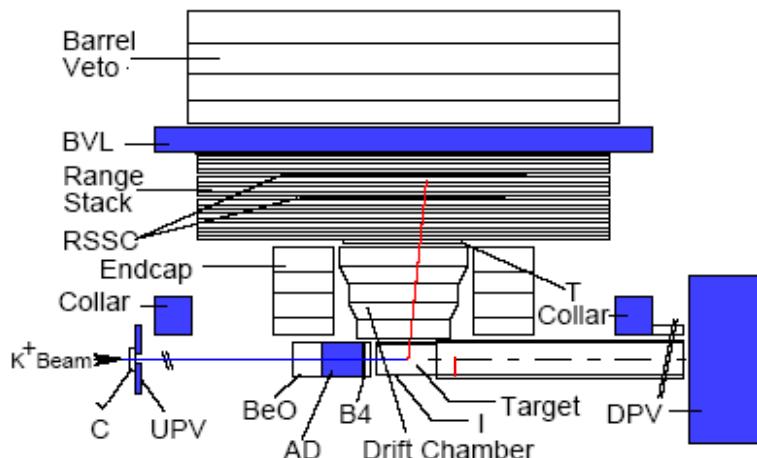
Background	BR ( $\times 10^{-3}$ )	Suppression method			
		PID	veto	TG	time
$K^+ \rightarrow \pi^+ \pi^0 (K_{\pi 2})$	209.2	-	✓✓	✓	-
$K^+ \rightarrow \pi^+ \pi^0 \gamma (K_{\pi 2\gamma})$	0.275	-	✓✓✓	-	-
$K^+ \rightarrow \pi^0 \mu^+ \nu (K_{\mu 3})$	33.2	✓	✓✓	-	-
$K^+ \rightarrow \mu^+ \nu \gamma (K_{\mu 2\gamma})$	6.2	✓	✓	-	-
$K^+ \rightarrow \pi^+ \pi^- e^+ \nu (K_{e 4})$	0.041	-	✓	✓	-
Beam backgrounds: single beam	-	✓	-	-	✓
double beam	-	-	✓✓	-	-
CEX: $K^+ n \rightarrow K^0 p$	$R_{K_L} = 2.8 \times 10^{-5}$	-	✓	✓	(✓)
$K_L^0 \rightarrow \pi^+ \mu^- \bar{\nu}$	135.0				
$K_L^0 \rightarrow \pi^+ e^- \bar{\nu}$	194.0				

# The beam



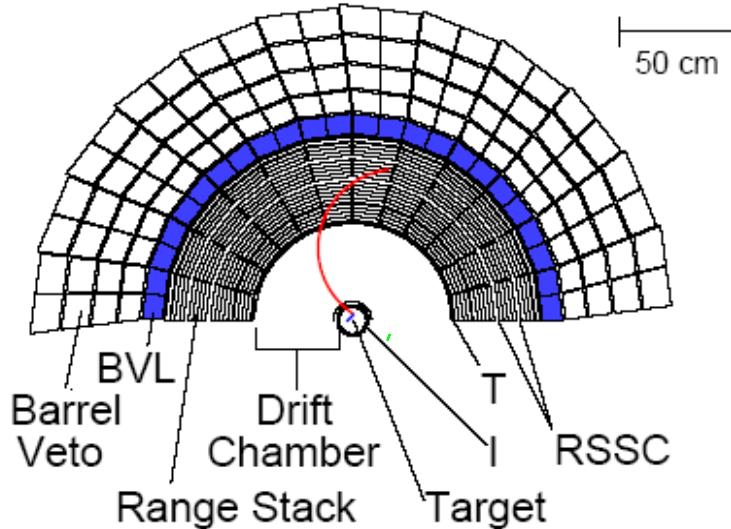
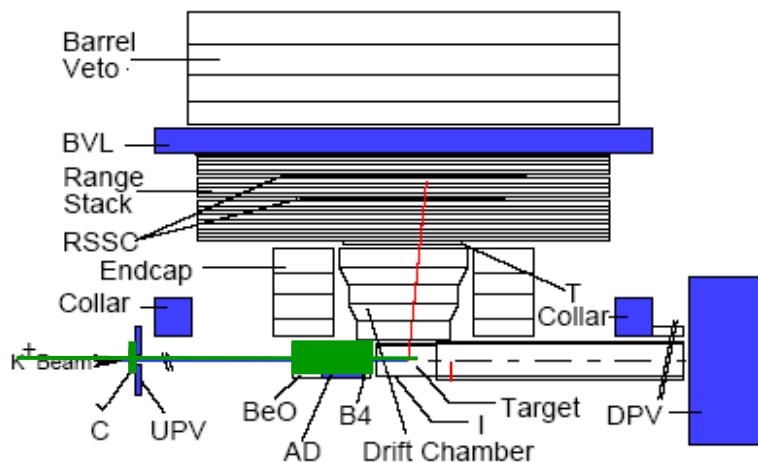
- The AGS extracts  $\sim 65 \times 10^{12}$  protons at  $22 \text{ GeV}/c$  over a  $2.2 \text{ sec}$  spill, every  $5.4\text{s}$
- They are shot on a platinum target and particles produced at  $\sim 0^\circ$  are sent to the Low Energy Separated Beamline (LESB III), where  $K^+$  are electrostatically separated from  $\pi^+$  and focused
- Finally in the E949 target,  $\sim 3.5 \times 10^6 K^+/\text{spill}$  arrive and stop, with a ratio of  $K/\pi \sim 2.5-3$

# The measurement w/ E949 detector



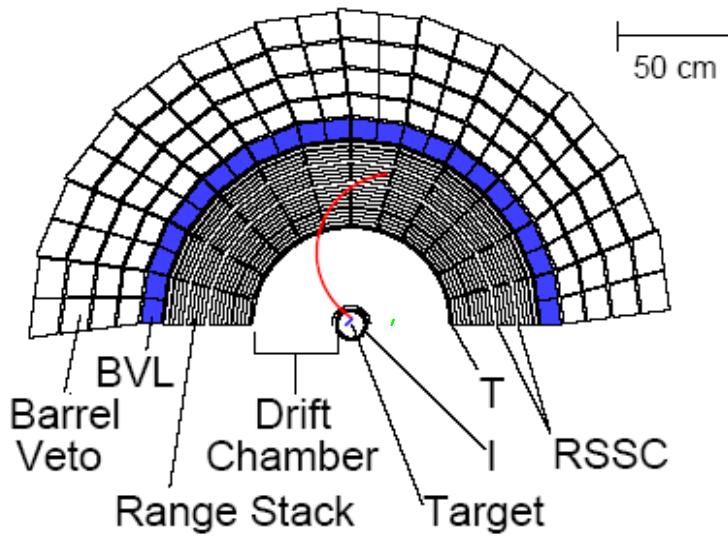
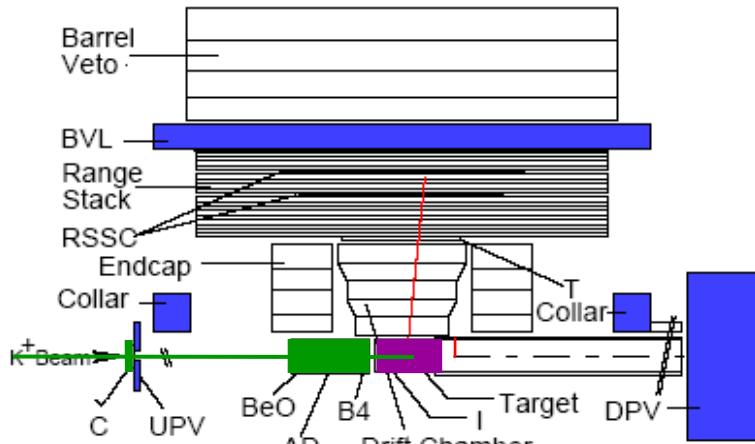
- Incoming 700MeV/c beam K<sup>+</sup>: identified by ckov, WC, scint. hodoscope (B4). Slowed down by BeO and AD
- K<sup>+</sup> stops & decays at rest in scintillating fiber target – measure delay (2ns)
- Outgoing  $\pi^+$  : verified by IC, VC, T counter. Momentum measured in UTC, energy & range in RS and target (1T magnetic field parallel to beam)
- $\pi^+$  stops & decays in RS – detect  $\pi^+ \rightarrow \mu^+ \rightarrow e^+$  chain
- Photons vetoed hermetically in BV-BVL, RS, EC, CO, USPV, DSPV
- New/upgraded elements

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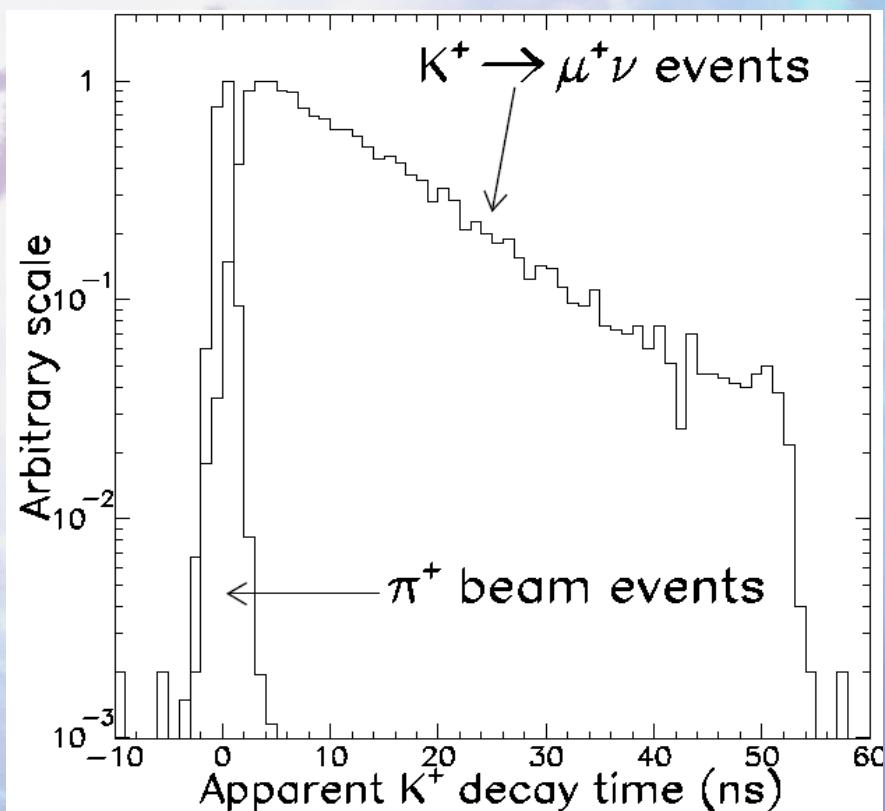


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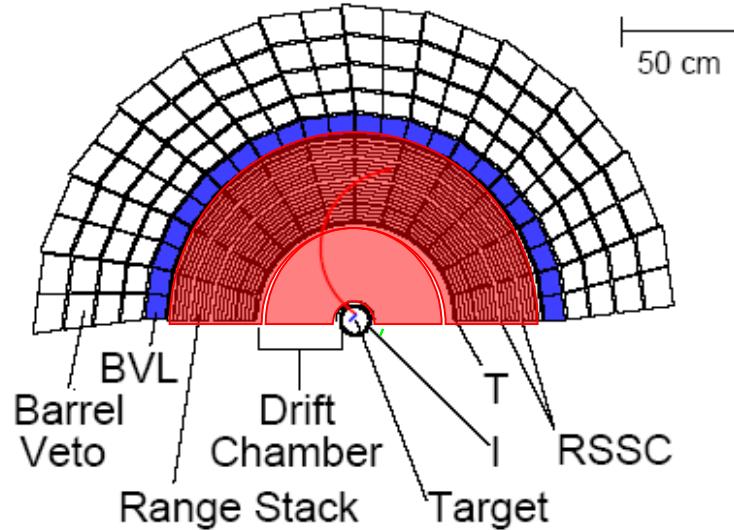
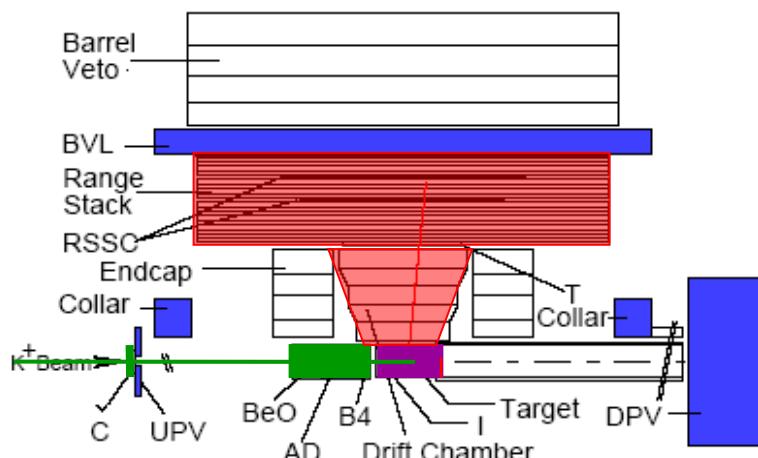
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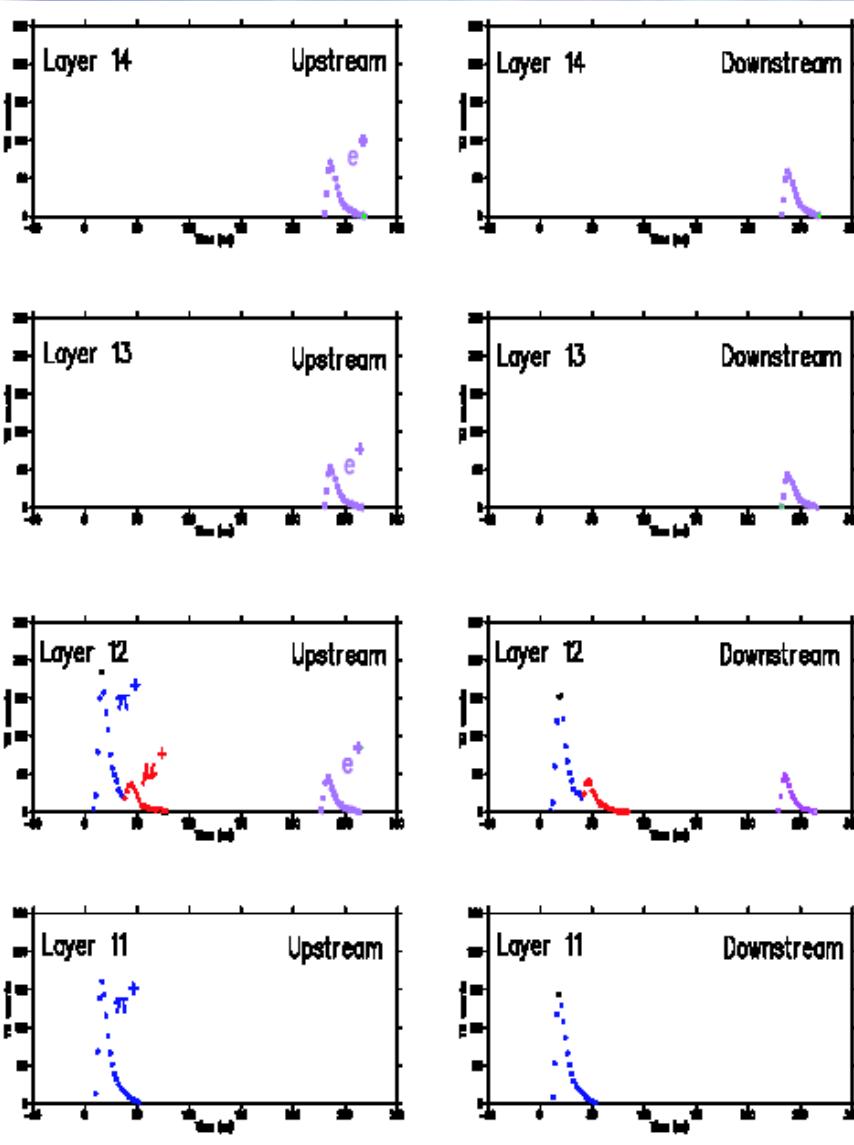


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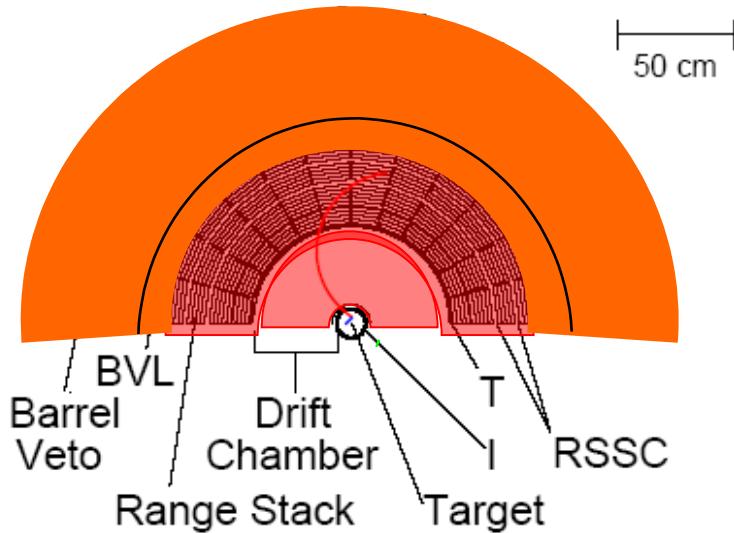
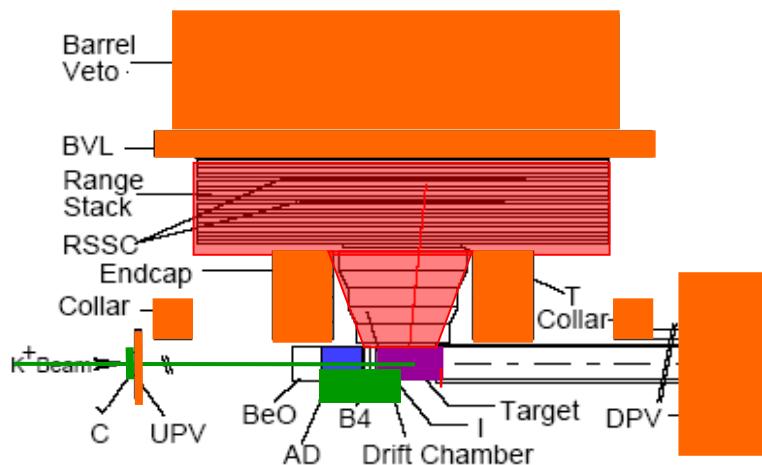
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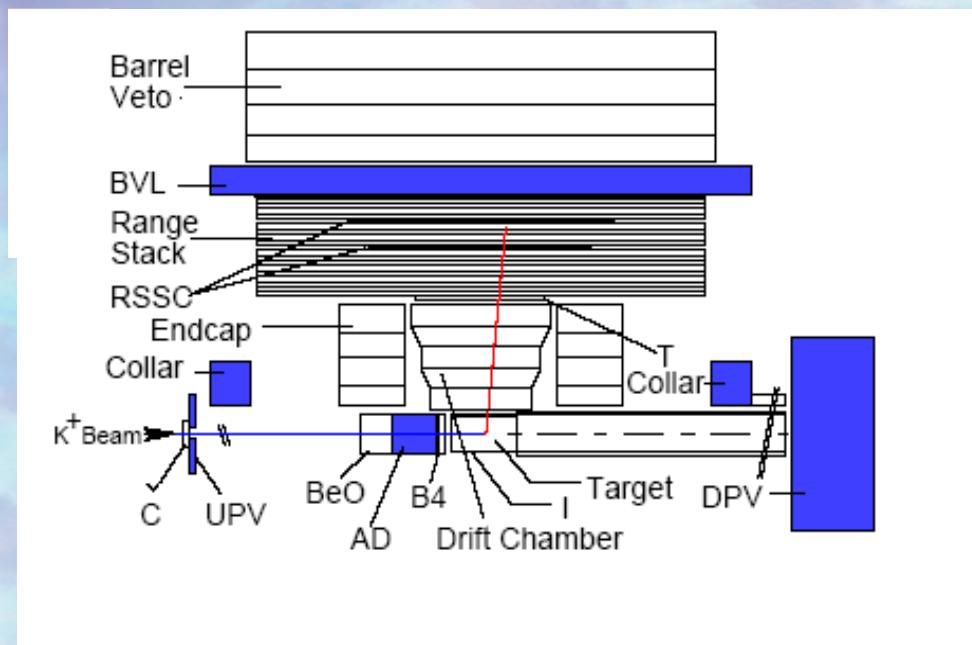
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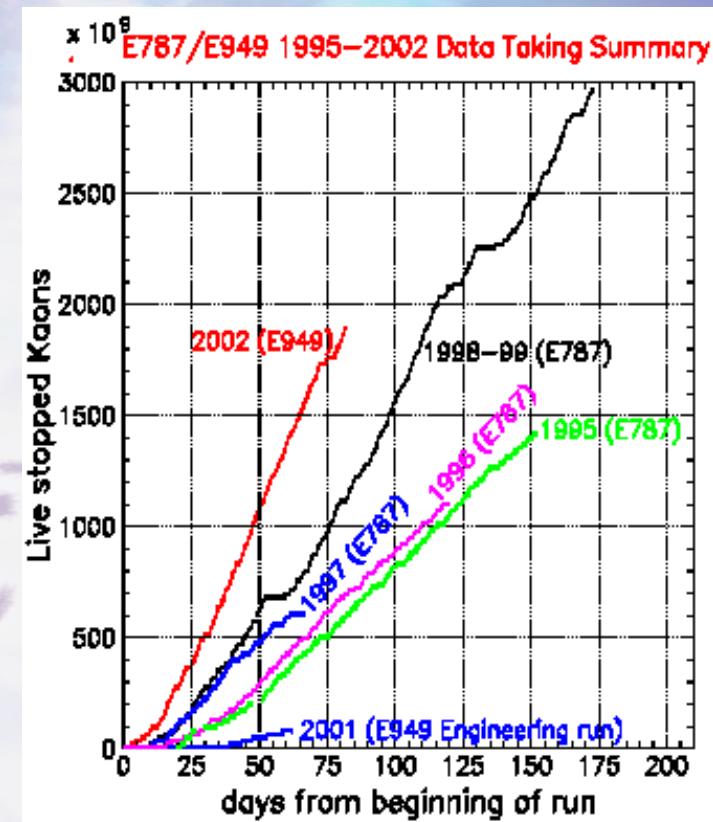


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# What's new in E949?



- ✓ New/upgraded PV elements
- ✓ More protons from AGS
- ✓ Improved tracking and energy resolution
- ✓ Higher rate capability due to DAQ, electronics and trigger improvements
- \* Lower beam duty factor
- \* Lower proton energy
- \* Problematic separators, worse  $K/\pi$  ratio

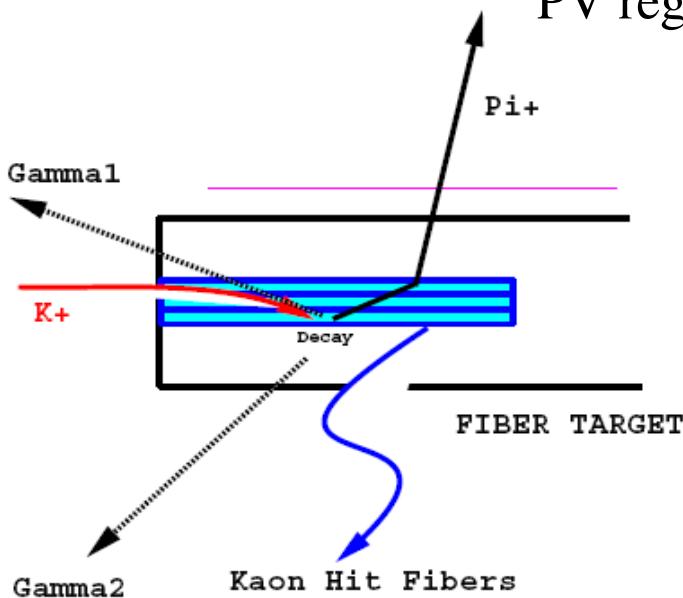


# Peculiarities of the PNN2 region

- ✓ More phase space than PNN1
- ✓ Probes different part of  $p_{\pi}$  spectrum → enhance validity of PNN1 result
- \* More backgrounds, difficult to disentangle from signal and from each other

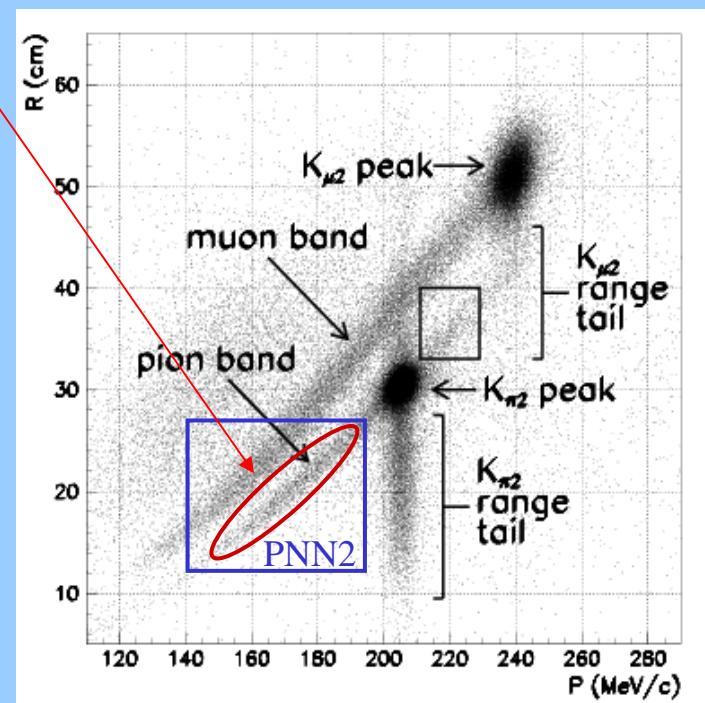
## Main background: Kp2 scatters in the Target

- Simultaneous shift in range AND momentum
- Photons head near beam direction, the weakest PV region of the detector



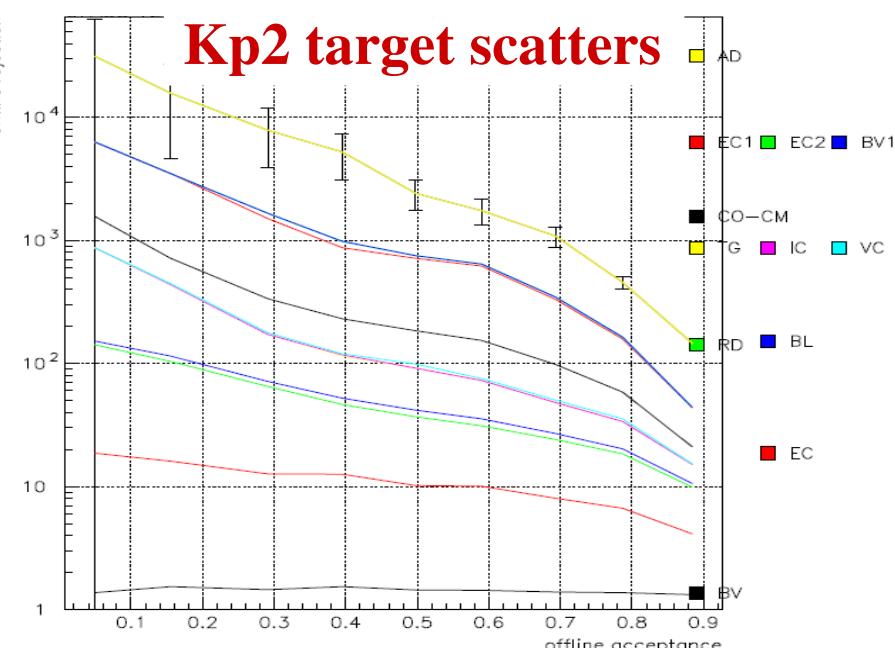
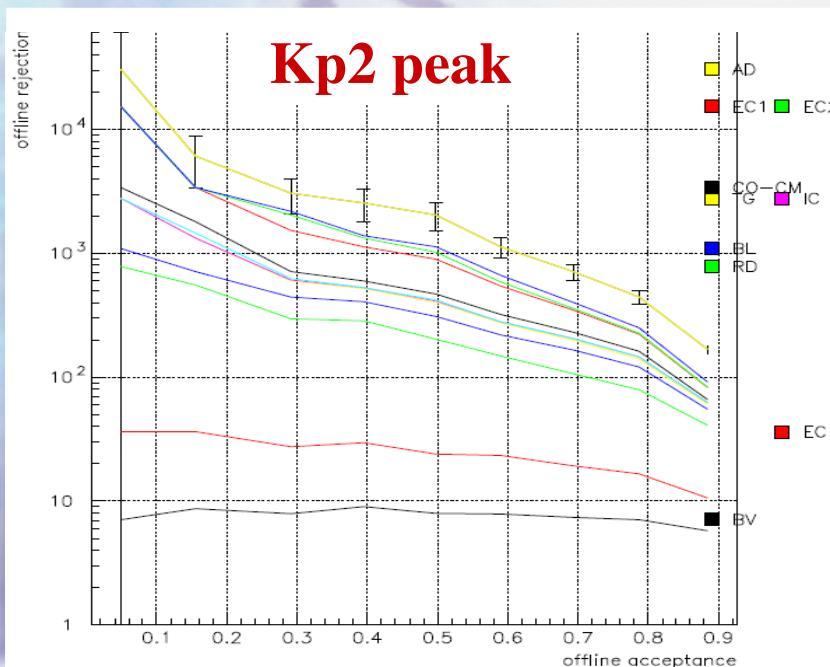
Decay product ( $\pi^+$  or  $\mu^+$ ) range in scintillator vs momentum:

- 2-body decay peaks
- multi-body decay and  $\pi^+$  scatter bands
- scattering tails



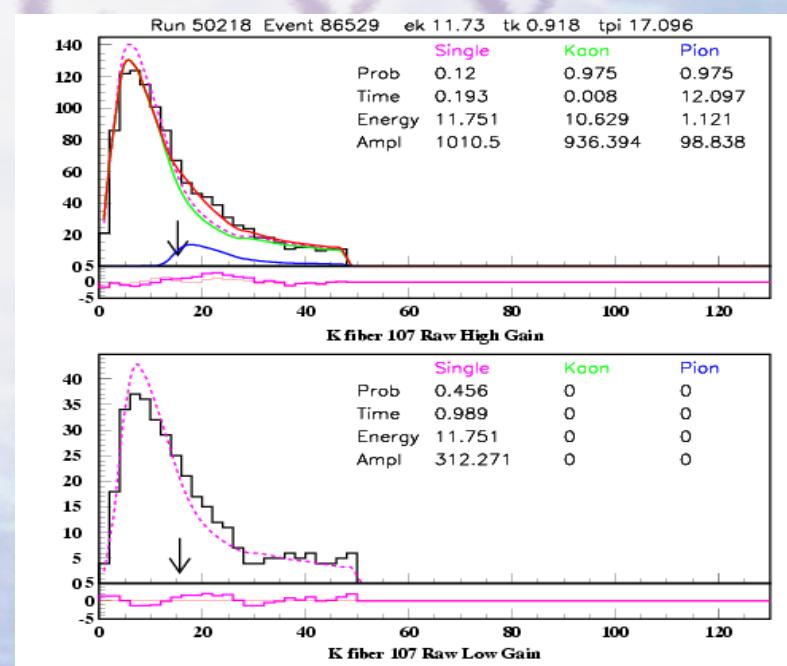
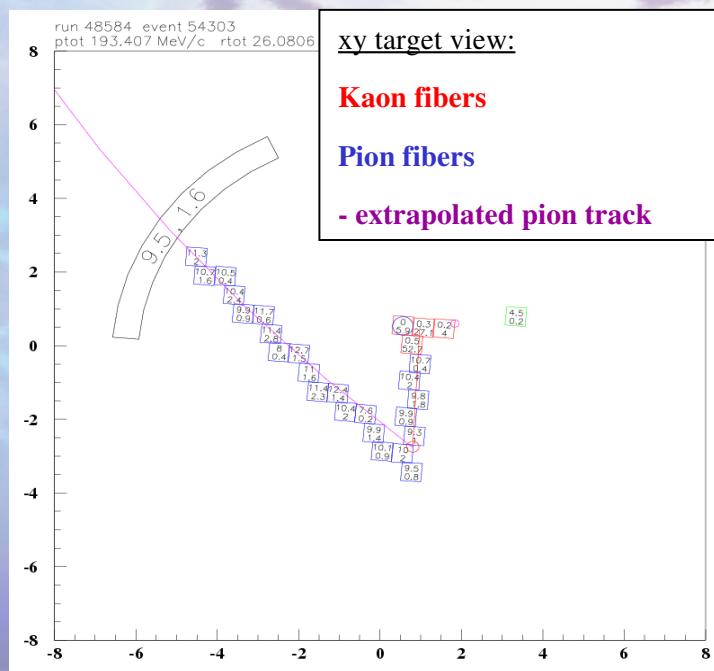
# Tools to suppress main background

- Improved Photon Veto, especially near the beam
  - Optimize at the Kp2 peak, check performance with xy-scatters
  - Measure rejection on different samples of scatters tagged by different “target quality” criteria  $\Rightarrow$  get a central value and the systematic error
- Improved algorithms to identify  $\pi^+$  scatters in target:
  - Transverse (xy-scatters) – pattern finding, fit quality
  - Longitudinal (z-scatters) – double pulse in the fiber due to the scatter, disagreement between TG and UTC information



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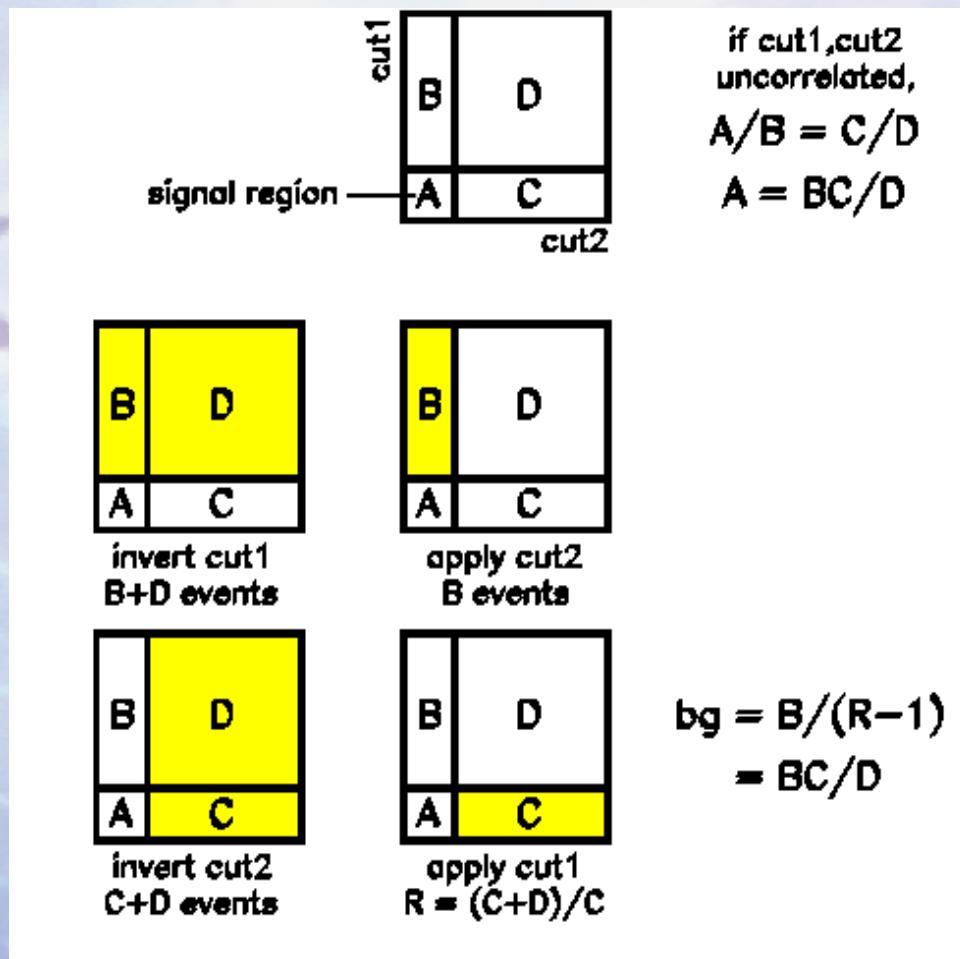
# Analysis strategy

- “Blind” analysis: don’t examine signal region until all backgrounds are verified
- To avoid bias, tune cuts using *randomly selected* 1/3 of the data, then measure background with remaining 2/3
- A priori identification of background sources
- Suppress each background source with at least two independent cuts

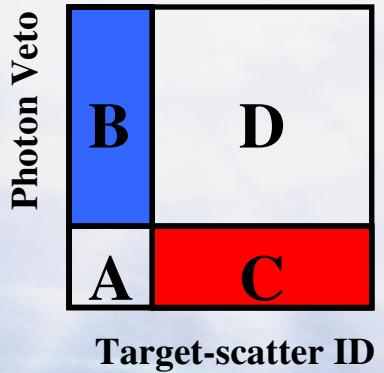
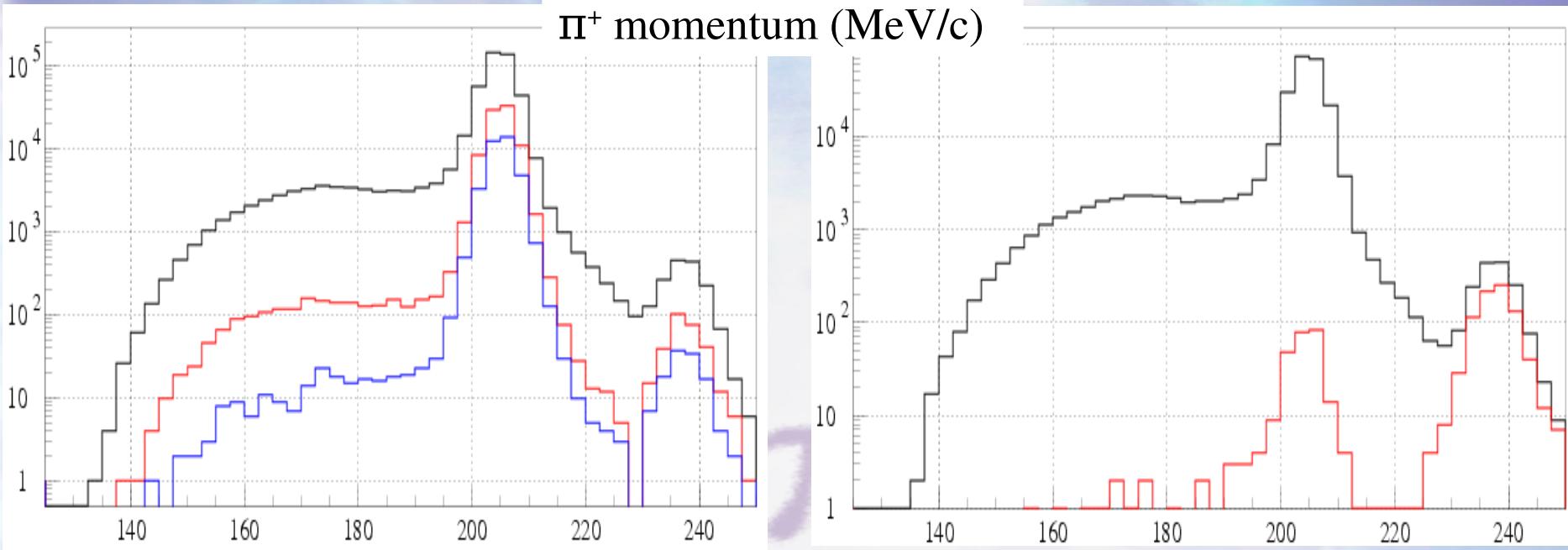
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		PID	veto	TG	time
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$K^+ \rightarrow \pi^o \mu^+ \nu (K_{\mu 3})$	33.2	✓	✓✓	-	-
$K^+ \rightarrow \mu^+ \nu \gamma (K_{\mu 2\gamma})$	6.2	✓	✓	-	-
$K^+ \rightarrow \pi^+ \pi^- e^+ \nu (K_{e4})$	0.041	-	✓	✓	-
Beam backgrounds: single beam	-	✓	-	-	✓
double beam	-	-	✓✓	-	-
CEX: $K^+ n \rightarrow K^o p$	$R_{K_L} = 2.8 \times 10^{-5}$	-	✓	✓	(✓)
$K_L^o \rightarrow \pi^+ \mu^- \bar{\nu}$	135.0				
$K_L^o \rightarrow \pi^+ e^- \bar{\nu}$	194.0				

# Bifurcated analysis

- Background cannot be reliably simulated  $\Rightarrow$  measure with data by inverting cuts and measuring rejection
- For backgrounds that cannot be reliably isolated in data, use MC to measure rejection and data for normalization



# $K^+ \rightarrow \pi^+ \pi^0$ TG scatters

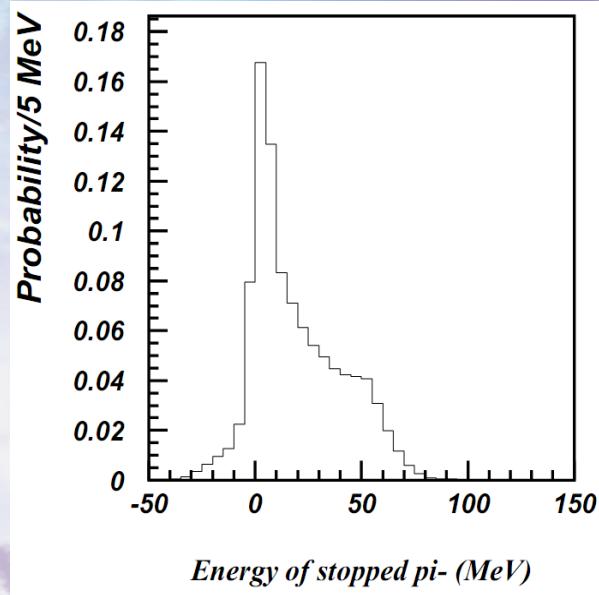
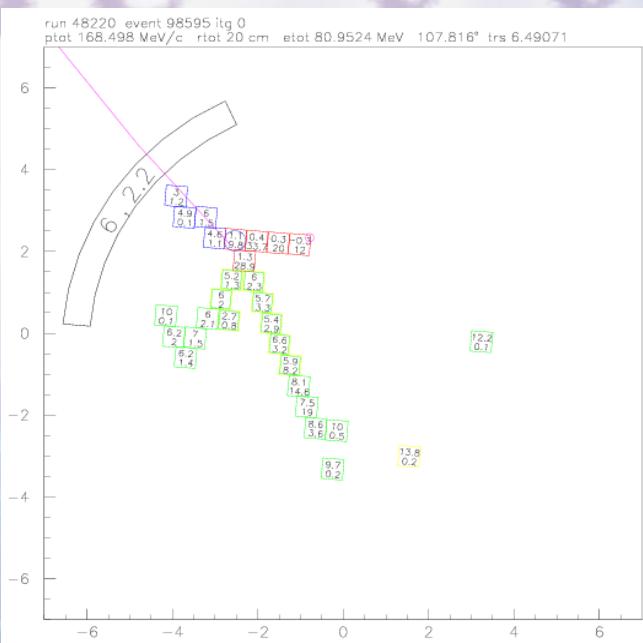
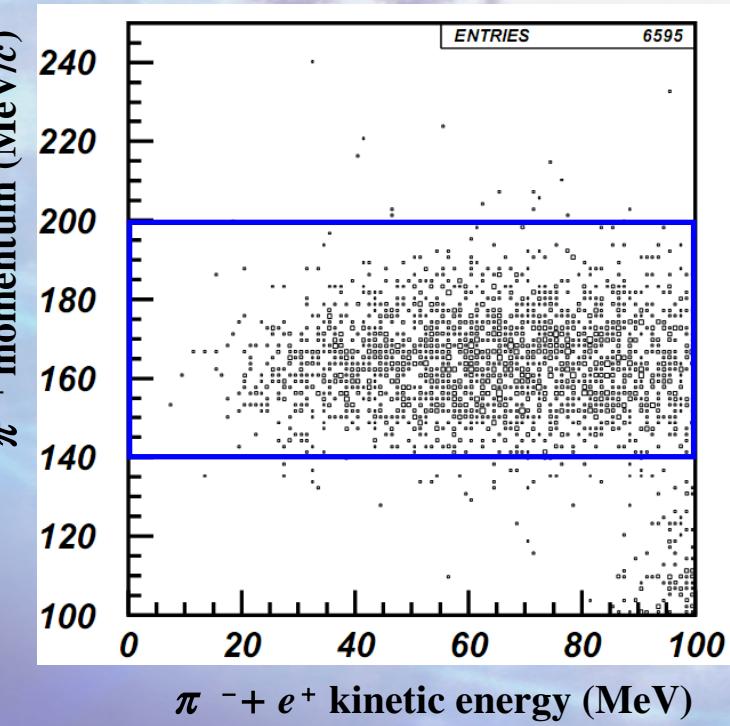


Select events with photons, apply target quality cuts  $\rightarrow$  region B

Select events with target scatter, apply PV  $\rightarrow$  measure rejection of photon veto  
 $(C+D)/C$

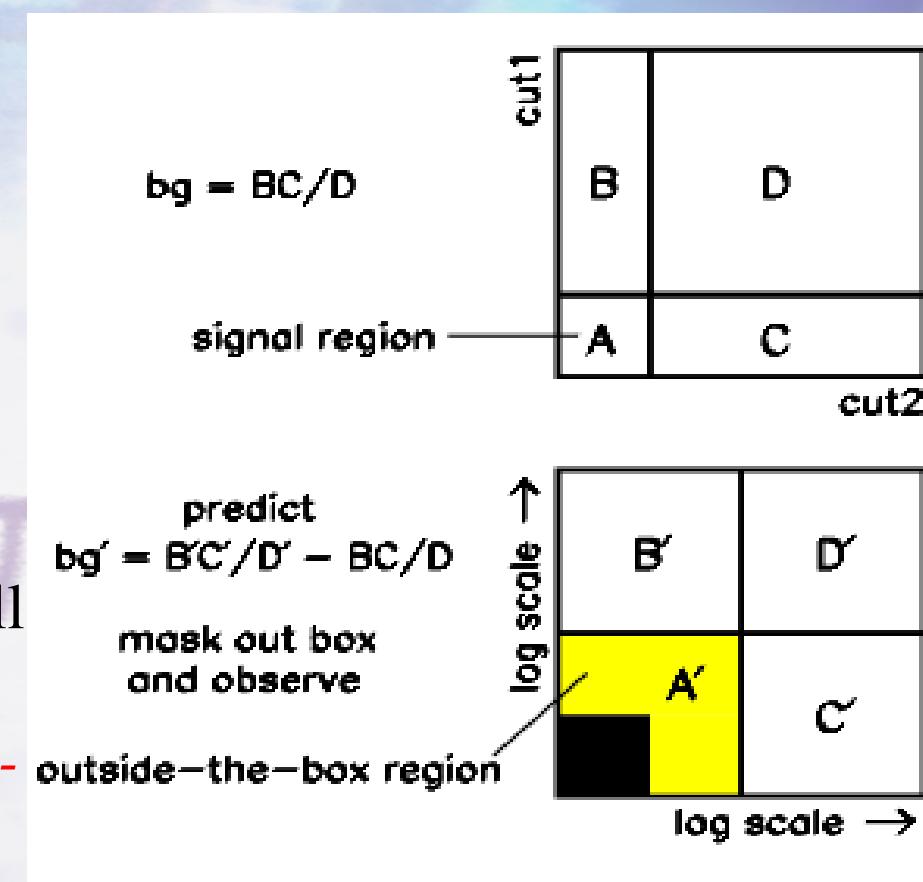
# $K^+ \rightarrow \pi^+ \pi^- e^+ \nu$

- Ke4 can be a background if the kinetic energy of the  $\pi^-$  and the  $e^+$  is low, so that they are not detected
- Isolate a pure Ke4 sample from data using target cuts, for normalization
- Find the rejection of those cuts from MC, which uses the measured energy deposit of the  $\pi^-$



# Cross-checks

- Verify background estimates and check for correlations by loosening cuts and comparing observed and predicted number of events remaining near the signal region (*“Outside-The-Box” study*)
- Examine events that failed only one or two (sets of) cuts, to make sure all background sources have been accounted for (*“Single- and Double-Cut-Failure” study*)



Region	$N_{\text{exp.}}$	$N_{\text{obs.}}$	$\mathcal{P}(N_{\text{obs.}}; N_{\text{exp.}})$	Combined
Target-scatter ID	$0.79^{+0.46}_{-0.51}$	0	0.45 [0.29,0.62]	N/A
Photon Veto 1	$9.09^{+1.53}_{-1.32}$	3	0.02 [0.01,0.05]	0.05 [0.02,0.14]
Photon Veto 2	$32.4^{+12.3}_{-8.1}$	34	0.61 [0.05,0.98]	0.14 [0.01,0.40]

# Expected background

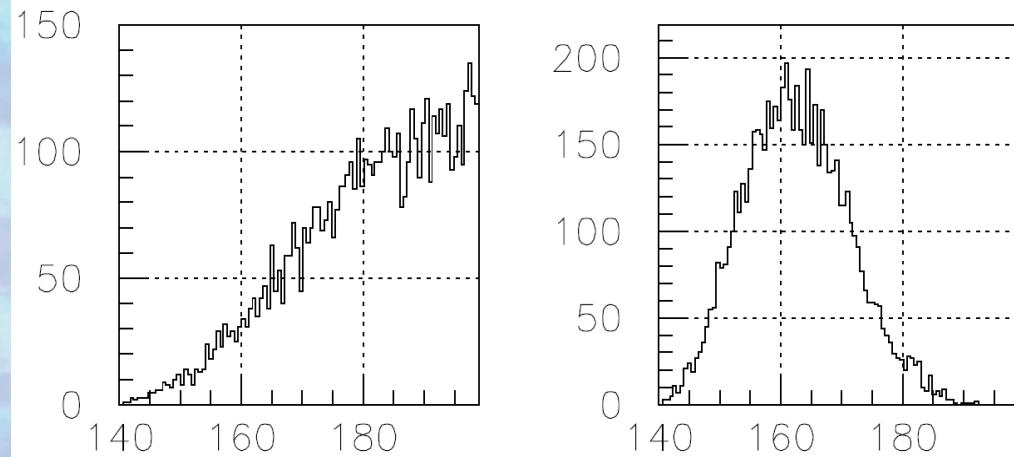
Process	Bkgd events (E949)	Bkgd events (E787)
$K_{\pi^2}$ -scatter	$0.649 \pm 0.150^{+0.067}_{-0.100}$	$1.030 \pm 0.230$
$K_{\pi^2\gamma}$	$0.076 \pm 0.007 \pm 0.006$	$0.033 \pm 0.004$
$K_{e4}$	$0.176 \pm 0.072^{+0.233}_{-0.124}$	$0.052 \pm 0.041$
CEX	$0.013 \pm 0.013^{+0.010}_{-0.003}$	$0.024 \pm 0.017$
Muon	$0.011 \pm 0.011$	$0.016 \pm 0.011$
Beam	$0.001 \pm 0.001$	$0.066 \pm 0.045$
Total bkgd	$0.93 \pm 0.17^{+0.32}_{-0.24}$	$1.22 \pm 0.24$
	E949 pnn2	E787 pnn2
Total Kaons	$1.70 \times 10^{12}$	$1.73 \times 10^{12}$
Total Acceptance	$1.37 \times 10^{-3}$	$0.84 \times 10^{-3}$
SES	$4.3 \times 10^{-10}$	$6.9 \times 10^{-10}$

Compared to the E787-PNN2 analysis, the total background decreased by 24% and total acceptance increased by 63%

# Division of signal region

- Signal and background are not uniformly distributed in the signal region  
⇒ A candidate in a cleaner region is less likely to be background

$\pi^+$  momentum (MeV/c) for signal and Ke4 background



- Divide signal region into 9 cells, by varying the PV, kinematic, muon ID and delayed coincidence cuts

rel. Acc	bkg	Acc/bkg
0.314	0.152	2.065
0.073	0.038	1.921
0.031	0.019	1.653
0.007	0.005	1.559
0.287	0.243	1.183
0.066	0.059	1.135
0.028	0.027	1.036
0.006	0.007	0.998
0.188	0.379	0.496
1	0.93	

# Likelihood ratio method

Calculate the BR using  $s_i/b_i$  of cells where event(s) are found, using the likelihood ratio method:

Maximize

$$X = \prod_{i=1}^n X_i, \quad X_i = \frac{e^{-(s_i + b_i)} (s_i + b_i)^{d_i}}{\frac{d_i!}{\frac{e^{-b_i} b_i^{d_i}}{d_i!}}}$$

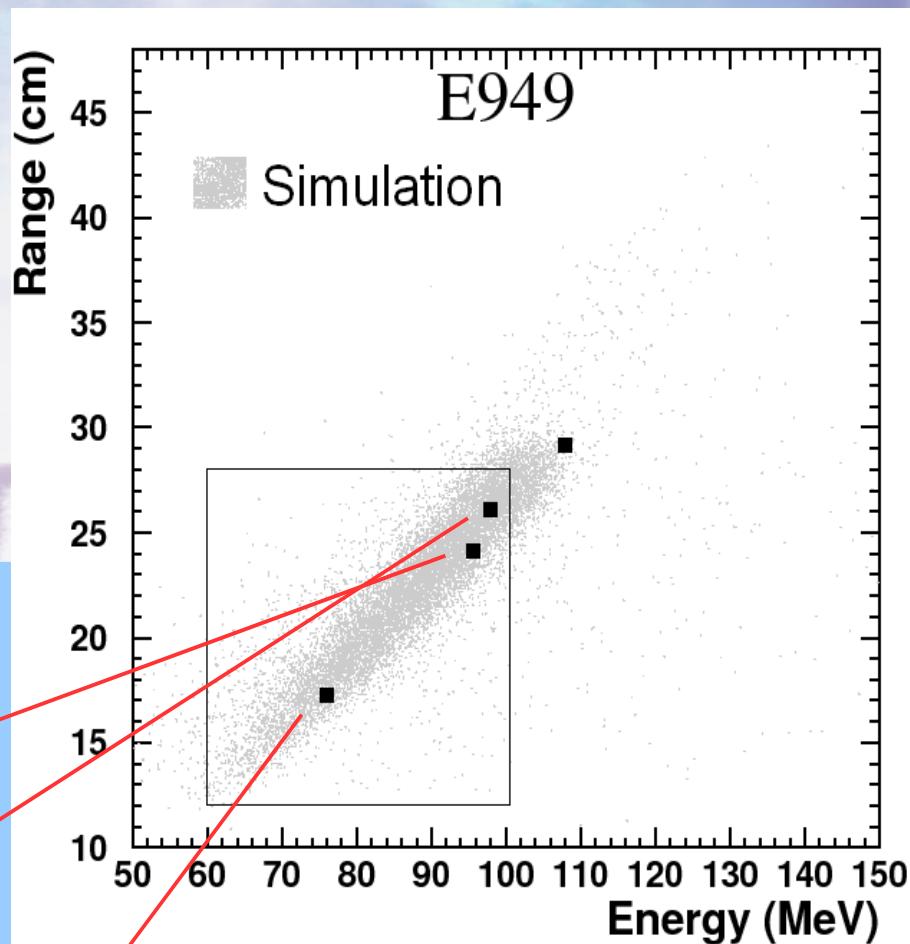
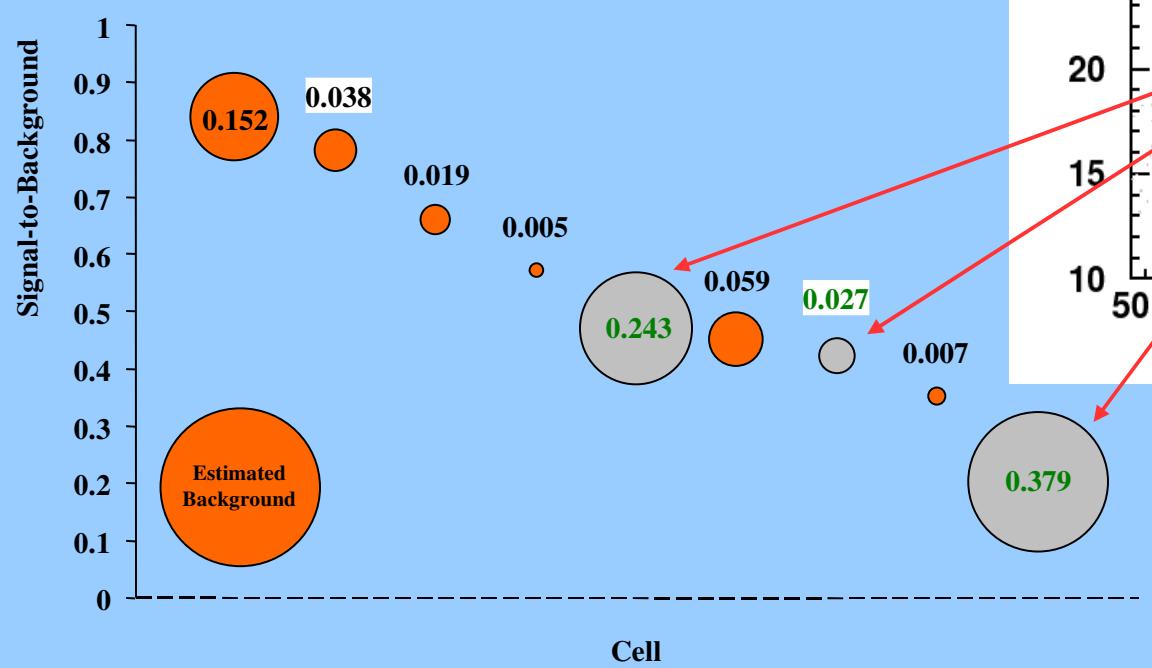
where  $d_i$  the number of candidates in cell  $i$ ,  $n$  the total number of cells

# Opening the box

# 3 candidate events found !

$$BR = (7.89^{+9.26}_{-5.19}) \times 10^{-10}$$

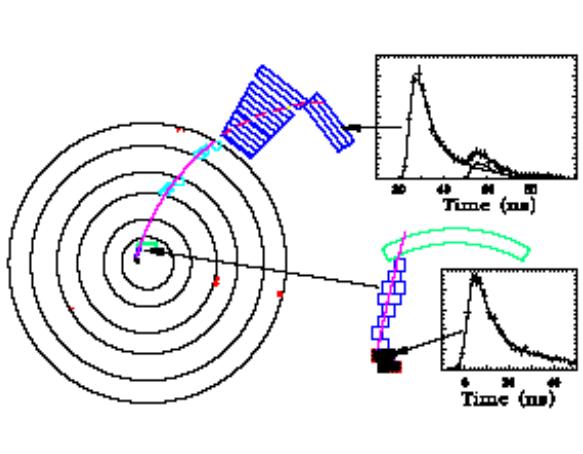
Probability that all 3 are due to background: **0.037**  
SM signal+background: **0.056**



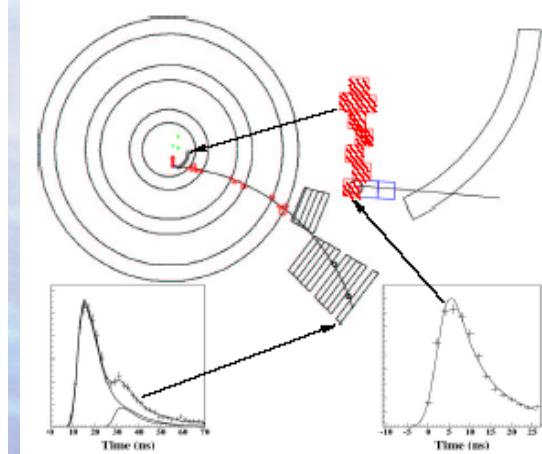
# Previous results

	E787		E949	
	PNN1	PNN2	PNN1	PNN2
<b>p(<math>\pi</math>) MeV/c</b>	[211,229]	[140,195]		[140,199]
<b>Stopped K<sup>+</sup></b>	$5.9 \times 10^{12}$	$1.7 \times 10^{12}$	$1.8 \times 10^{12}$	$1.7 \times 10^{12}$
<b>Background</b>	$0.14 \pm 0.05$	$1.22 \pm 0.24$	$0.30 \pm 0.03$	$0.93 \pm 0.17$
<b>Acceptance</b>	0.0020	0.0008	0.0022	0.0014
<b>S.E.S.</b>	$0.8 \times 10^{-10}$	$6.9 \times 10^{-10}$	$2.6 \times 10^{-10}$	$4.3 \times 10^{-10}$
<b>Candidates</b>	2	1	1	3
<b>BR (<math>\times 10^{-10}</math>)</b>	$1.57^{+1.75}_{-0.82}$	<22 (90% CL)	$1.47^{+1.30}_{-0.89}$	$1.73^{+1.15}_{-1.05}$

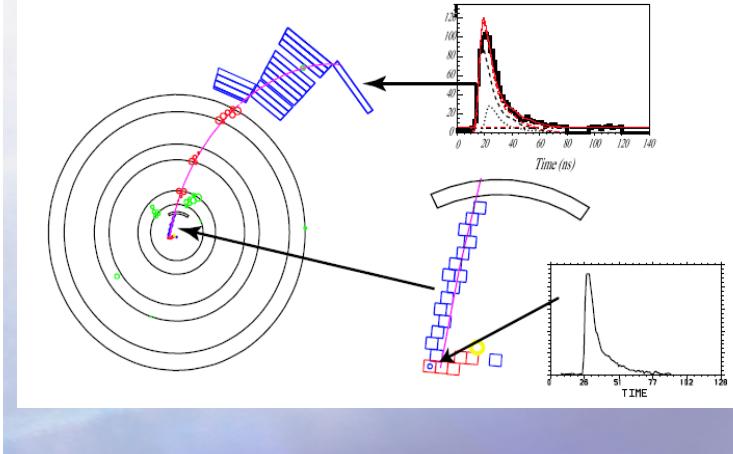
Candidate E787A



Candidate E787C



Candidate E949A

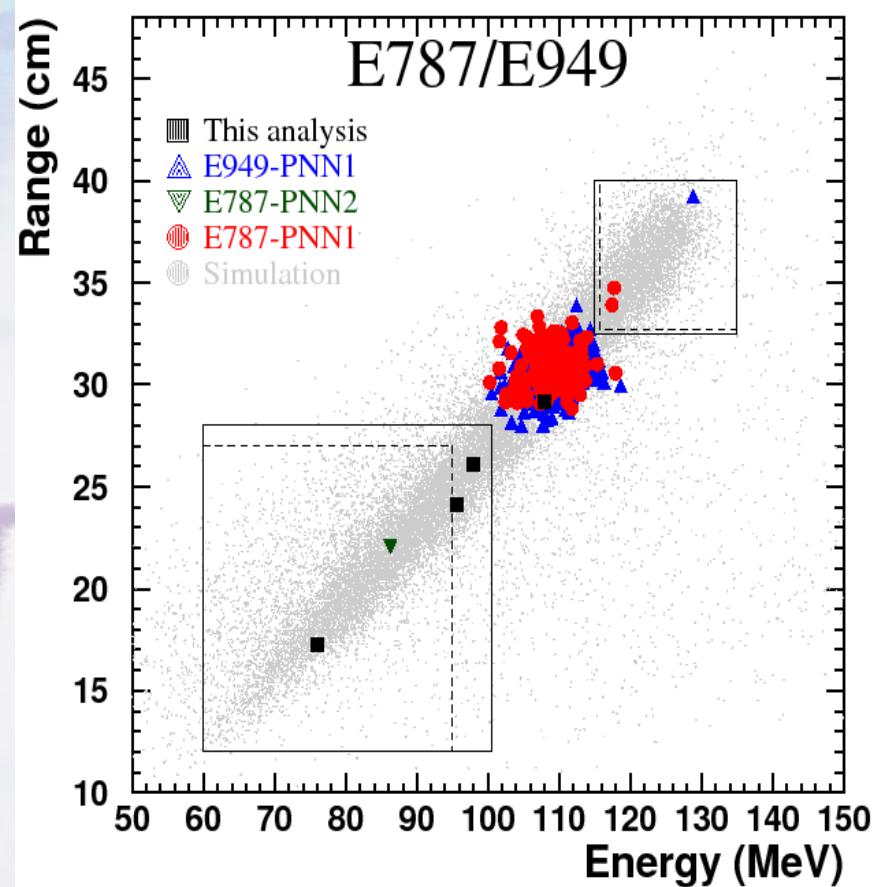


# Combined result

**7 candidate events in total**

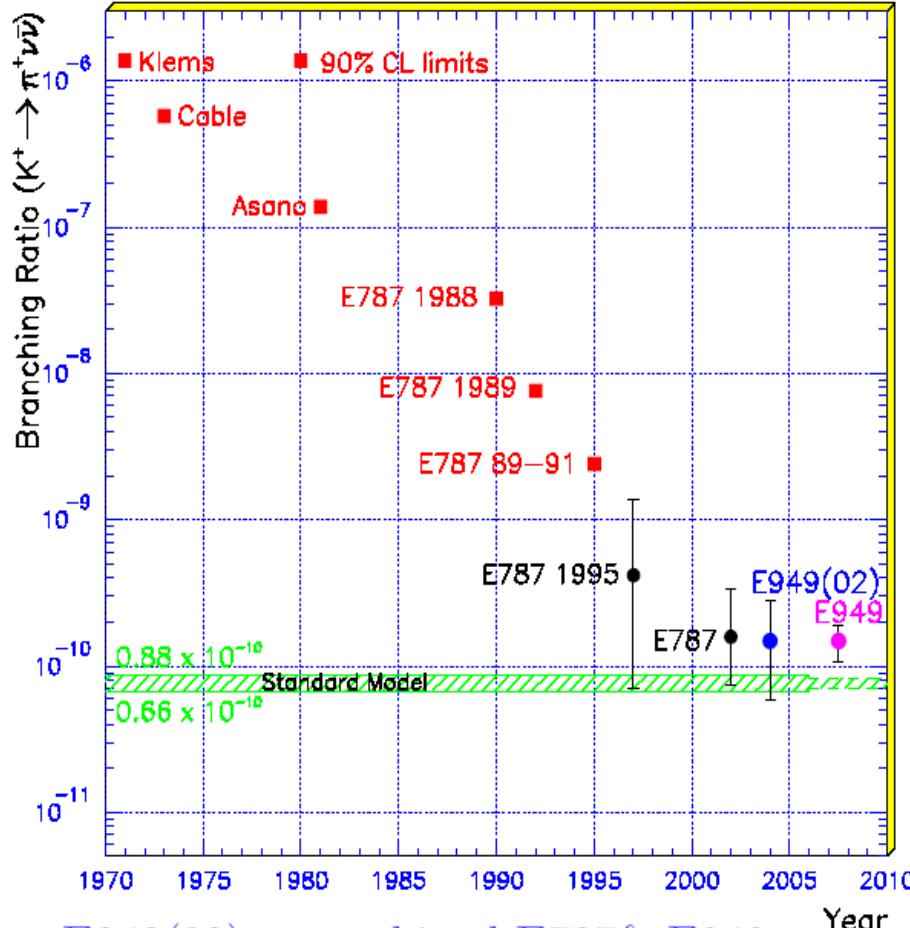
$$BR = (1.73^{+1.15}_{-1.05}) \times 10^{-10}$$

Probability that all 7 are due to background: **0.001**  
SM signal+background: **0.060**



*Central value, although still  $\sim 2 \times$  SM, it is consistent with it within errors...*

# Progress and future prospects



E949(02) = combined E787& E949.

E949 projection with full running period.

- Obviously, more statistics are needed → it would have been nice if E949 had all its promised running time...
- Fortunately others have taken over: NA62 at CERN, E391a at JPARC, Project X at Fermilab(?)

- E787 upgrade into E949 worked as expected
- Final bit of the puzzle is now in place (PNN2 measurement), and E787/E949 have a final and definitive result
- Thanks to detector upgrades and deeper understanding of the analysis techniques, the PNN2 study was fruitful and observed 3 candidate events with an expected background of ~1
- The combined BR measured by E787/E949 in both kinematic regions is  $BR(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (1.73^{+1.15}_{-1.05}) \times 10^{-10}$ , which is still consistent with the SM
- More experiments are running or are under preparation, set to constrain the CKM parameters from the Kaon sector – *good luck!*

# Extras

# CKM matrix

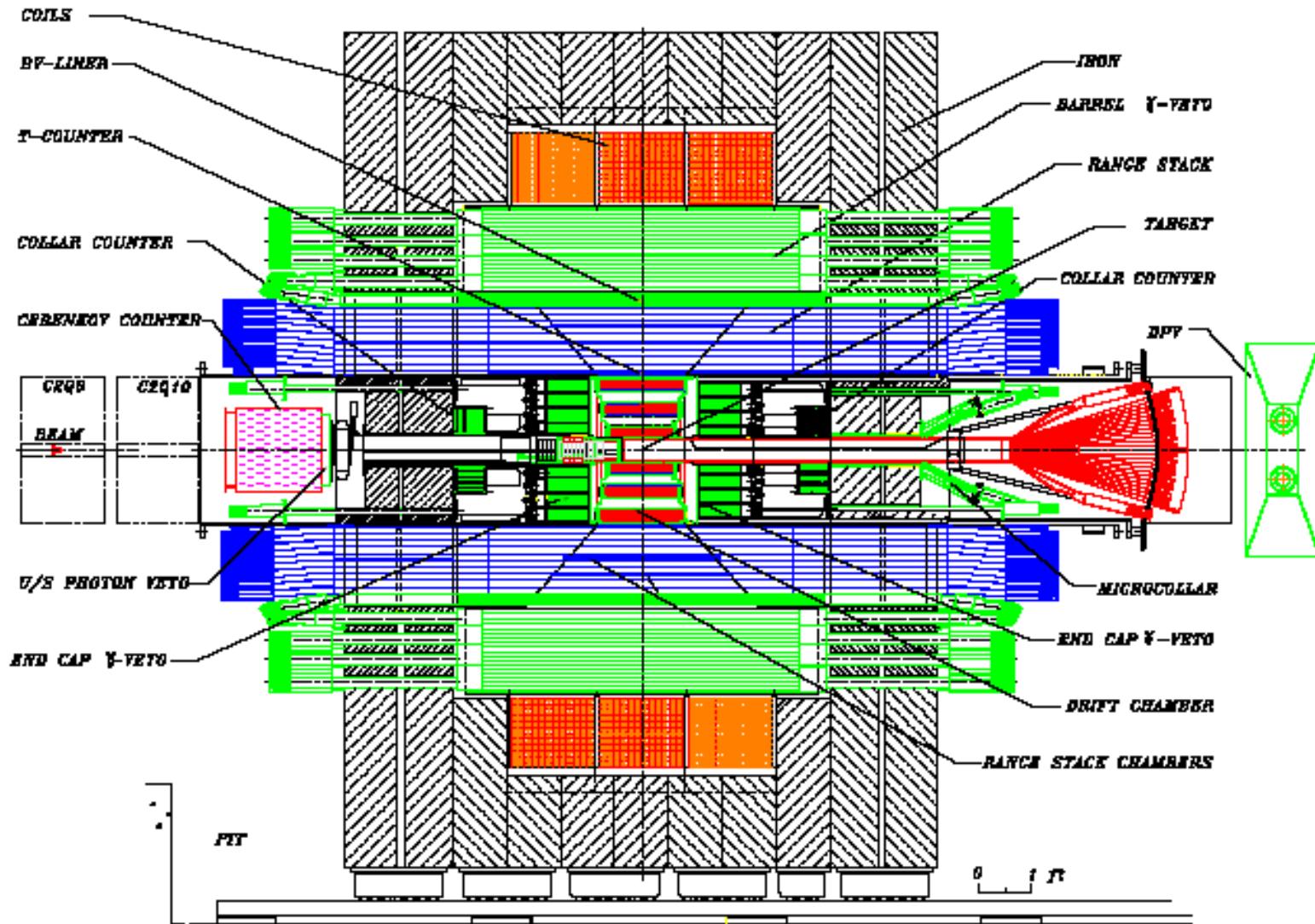
The CKM matrix relates weak with mass eigenstates. In the Wolfenstein parametrization,

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 - \frac{\lambda^2}{2} & \lambda & A \lambda^3 (\rho - i \eta) \\ -\lambda & 1 - \frac{\lambda^2}{2} & A \lambda^2 \\ A \lambda^3 (1 - \bar{\rho} - i \bar{\eta}) & -A \lambda^2 & 1 \end{pmatrix}$$

where  $\bar{\rho} = \rho \left(1 - \frac{\lambda^2}{2}\right)$  ,  $\bar{\eta} = \eta \left(1 - \frac{\lambda^2}{2}\right)$

**CP violation** arises from the irreducible phase of  $V_{CKM}$  , because it's 3x3 (3 generations)

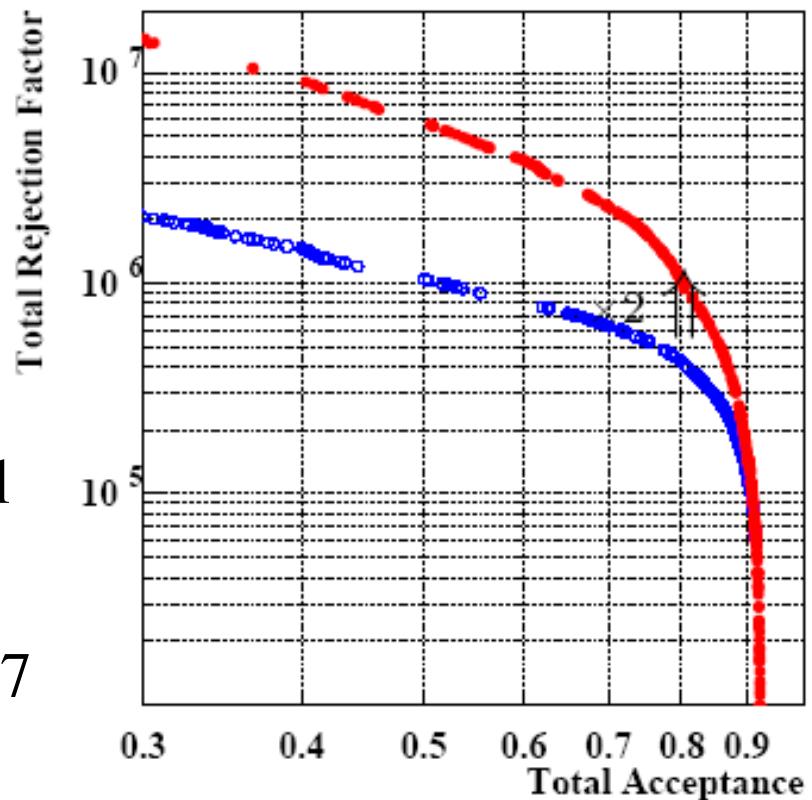
# The E949 detector



# Photon Veto improvement

~  $2 \times$  better rejection at nominal PNN1 acceptance (80%) or

~ 5% more acceptance with E787 rejection !



\* Good news for PNN2 as well...

E787, E949

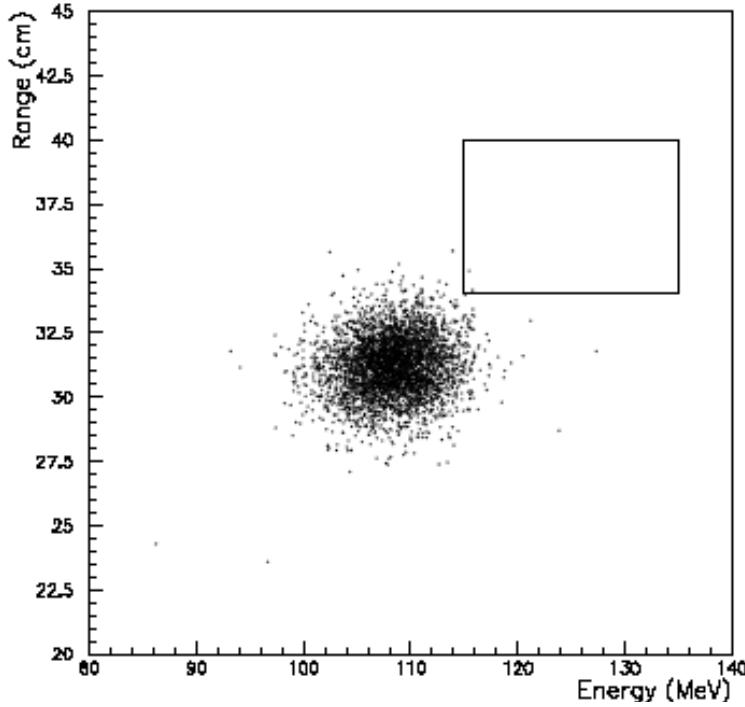
# Analysis strategy (1)

- “Blind” analysis: don’t examine signal region until all bg are verified
- To avoid bias, tune cuts using *randomly selected* 1/3 of the data, then measure bg with remaining 2/3
- A priori identification of bg sources
- Suppress each bg source w/ at least two independent cuts
- Bg cannot be reliably simulated  $\Rightarrow$  measure w/ data by inverting cuts and measuring rejection

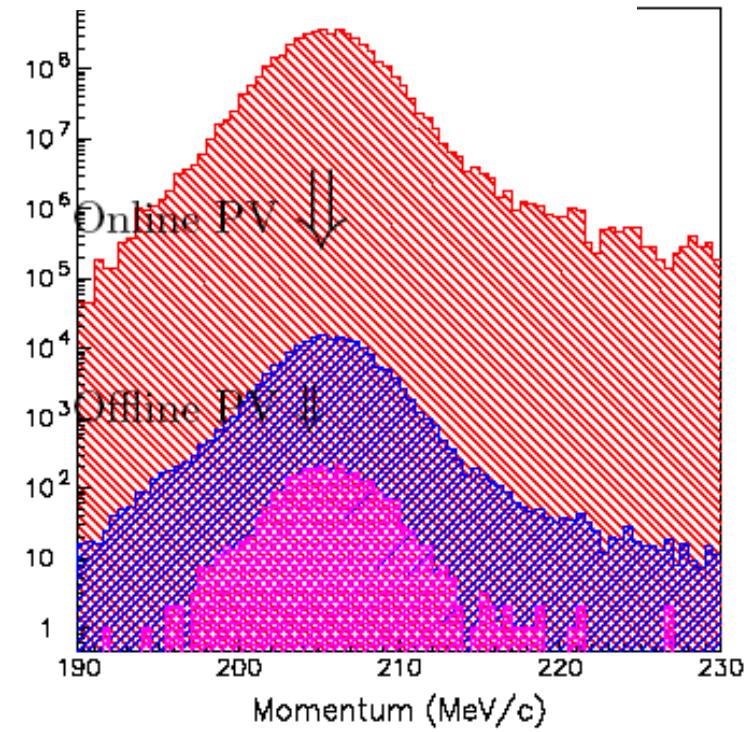
Source	Suppression method			
	Kinematics	Particle ID	Veto	Timing
$K^+ \rightarrow \mu^+ \nu(\gamma)$ ( $K_{\mu 2}$ )	✓	✓	(✓)	
$K^+ \rightarrow \pi^+ \pi^0$ ( $K_{\pi 2}$ )	✓		✓	
Scattered $\pi^+$ beam		✓		✓
CEX			✓	✓

$$\text{CEX} \equiv K^+ n \rightarrow K^0 p , K_L^0 \rightarrow \pi^+ \ell^- \nu$$

# Example: $K^+ \rightarrow \pi^+\pi^0$ bg rejection



Select events with photons, measure  
rejection of kinematic cuts (P, R, E  
“box”)



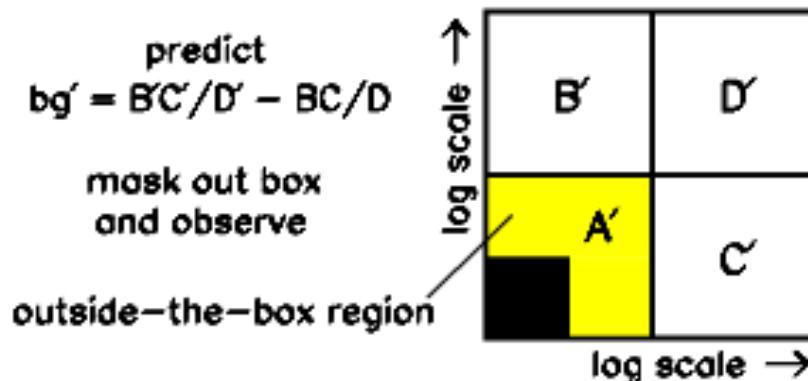
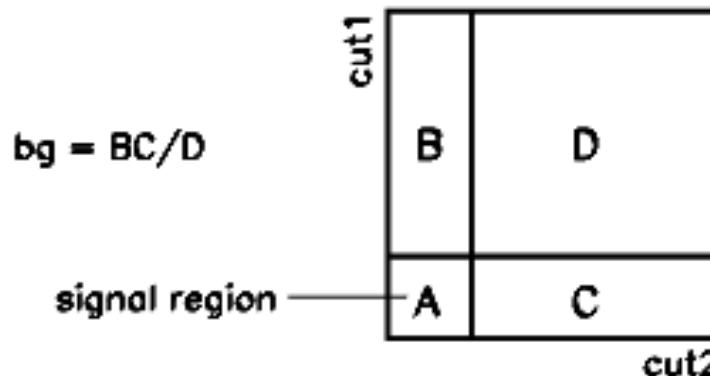
Select  $K^+ \rightarrow \pi^+\pi^0$  kinematically, measure  
rejection of photon veto

# Analysis strategy (2)

- Verify bg estimates & check for correlations by loosening cuts and comparing observed and predicted number of events remaining.
- Construct **background functions** by varying *one cut at a time*, keeping the other inverted. Use them to estimate bg in the signal region.
- Use MC to measure geometrical acceptance, verify by measuring  $\text{BR}(\text{K}^+ \rightarrow \pi^+ \pi^0)$

# Analysis strategy (3)

- Verify bg estimates & check for correlations by *simultaneously* loosening both cuts and comparing observed and predicted number of events remaining. Construct **background functions** by varying *one cut at a time*, keeping the other inverted.



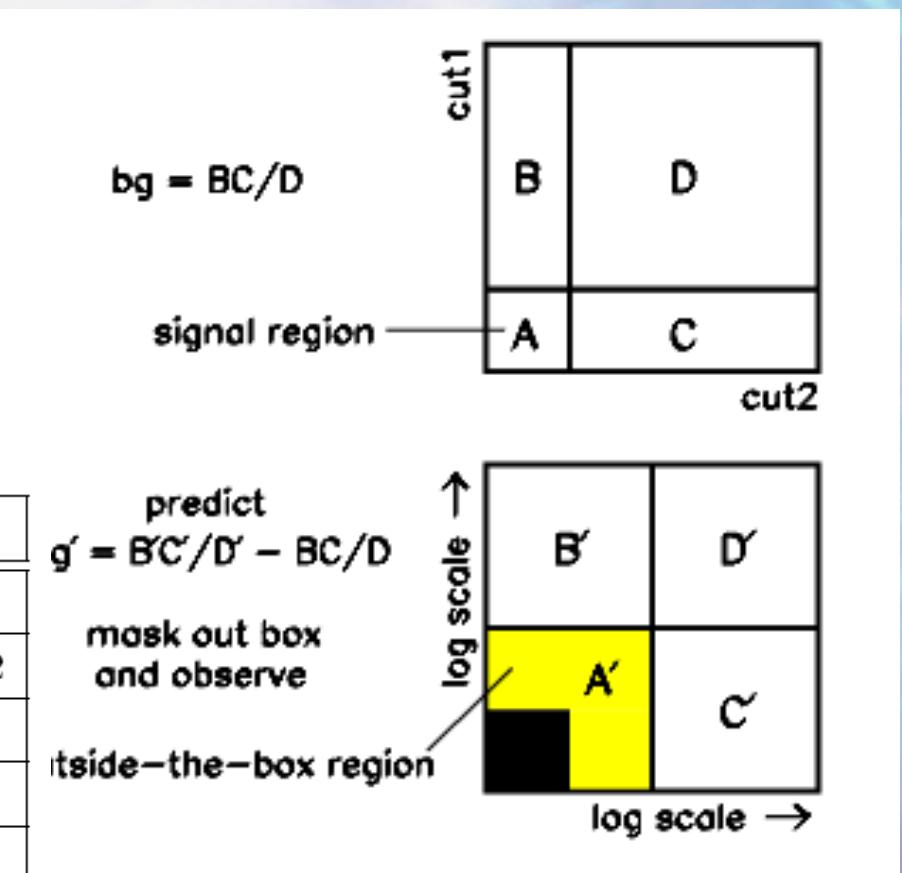
# OTB study & acceptance measurement

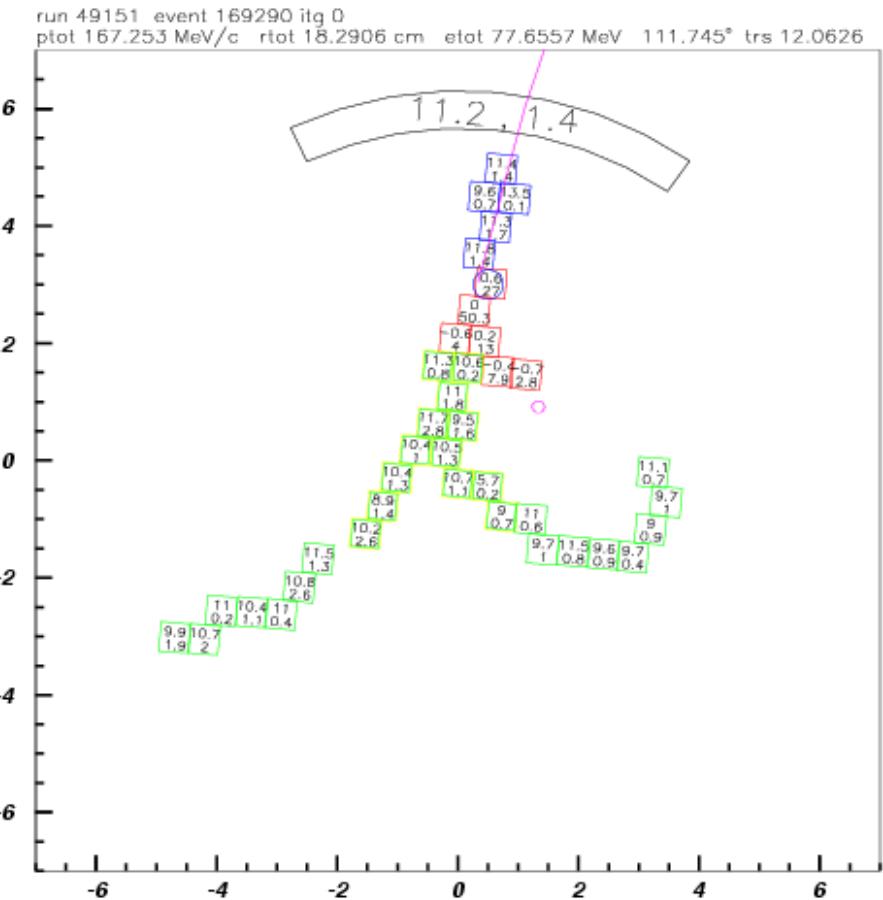
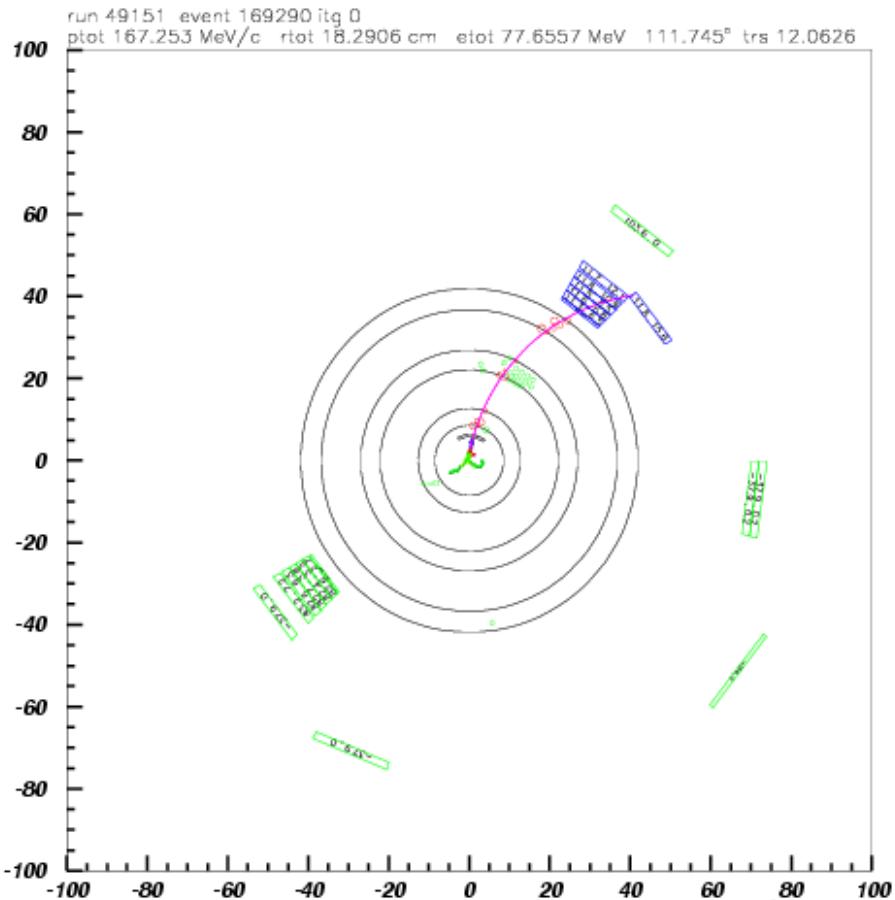
- Verify bg estimates & check for correlations by loosening cuts and comparing observed and predicted number of events remaining (“outside-the-box” study).

## Acceptance measurement:

- Use special background samples (with loose trigger) to measure cuts' and part of trigger acceptance
- Use signal MC to measure geometrical acceptance

	E787		E949
Stopped K <sup>+</sup> ( $N_K$ )	$5.9 \times 10^{12}$		$1.8 \times 10^{12}$
Total Acceptance	$0.0020 \pm 0.0002$		$0.0022 \pm 0.0002$
S.E.S.	$0.8 \times 10^{-10}$		$2.6 \times 10^{-10}$
Total Background	$0.14 \pm 0.05$		$0.30 \pm 0.03$
Candidate	E787A	E787C	<b>E949A</b>
$S_i/b_i$	50	7	<b>0.9</b>
$W_i \equiv \frac{S_i}{S_i + b_i}$	0.98	0.88	<b>0.48</b>





$K^+ \rightarrow \pi^+ \pi^0$  TG scatter event